

<b>1E2002</b>	Roll No. _____	Total No of Pages: <b>3</b>
<b>1E2002</b>		
<b>B. Tech I Sem. (Main/Back) Exam. Jan. 2016</b>		
<b>102 Engineering Mathematics-I</b>		
<b>Common to all Branches</b>		

**Time: 3 Hours**

**Maximum Marks: 80**  
**Min. Passing Marks: 24**

*Instructions to Candidates:*

*Attempt any **five** questions, selecting **one** question from each unit. All questions carry **equal** marks. Schematic diagrams must be shown wherever necessary. Any data you feel missing suitably be assumed and stated clearly.*

*Units of quantities used/calculated must be stated clearly.*

*Use of following supporting material is permitted during examination.*

1. NIL

2. NIL

### UNIT-I

Q.1 (a) Find the asymptotes of the curve

$$x^3 - 5x^2y + 8xy^2 - 4y^3 + 2y^2 + x^2 - 3xy - 1 = 0. \quad [8]$$

(b) Show that the radius of curvature at any point P on the parabola  $y^2 = 4ax$ , is

$$\frac{2(SP)^{3/2}}{\sqrt{a}}; \text{ where S is the focus of the parabola.} \quad [8]$$

### OR

Q.1 (a) Prove that the curve  $x^3 + y^3 = a^3$  has point of inflexion at the point of inflexion at the points where it crosses the co-ordinate axes. [8]

(b) Trace the curve  $r = a(1 + \cos\theta)$ . (Cardioid). [8]

**UNIT-II**

Q.2 (a) If  $u = \tan^{-1}\left(\frac{x^3 + y^3}{x + y}\right)$ , then show that

$$x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2} = \sin 2u (1 - 4\sin^2 u) \quad [8]$$

(b) If measurements of radius of base and height of a right circular cone are incorrect by -1% & 2% respectively, find the error in its volume. [8]

**OR**

Q.2 (a) Find the minimum value of  $x^2 + y^2 + z^2$ , given that  $ax + by + cz = p$  [8]

(b) Find the volume of the greatest rectangular parallelopiped inscribed in the ellipsoid whose equation is  $\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$  [8]

**UNIT-III**

Q.3 (a) Find the surface area of the solid formed by revolving the ellipse

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1, \text{ about the major axis.} \quad [8]$$

(b) Find the volume of the solid generated by revolving the curve  $(a-x)y^2 = a^2x$ , about its asymptote. [8]

**OR**

Q.3 (a) Change the order of integration in the integral  $\int_0^a \int_{\left\{ \begin{array}{l} a + \sqrt{a^2 - y^2} \\ a - \sqrt{a^2 - y^2} \end{array} \right\}} xy \, dx \, dy$  and then

evaluate it. [8]

(b) Show that  $\int_0^{\infty} \frac{x^2 dx}{(1+x^4)^3} = \frac{5\pi\sqrt{2}}{128}$ . [8]

**UNIT-IV**

Q.4 (a) Solve:-

(i)  $(1+y^2) + \left(x - e^{-\tan^{-1}y}\right) \frac{dy}{dx} = 0.$  [5]

(ii)  $x \frac{dy}{dx} + y = y^2 \log x.$  [5]

(b)  $(D^2 + 1)^2 y = 24x \cos x$  ;  $D = d/dx$ , Solve it. [6]

**OR**

Q.4 (a) Solve:

(i)  $(3x^2 + y/x) dx + (x^3 + \log x) dy = 0$  [5]

(ii)  $(xy \sin xy + \cos xy) y dx + (xy \sin xy - \cos xy) x dy = 0.$  [5]

(b) Solve:

$\frac{d^2x}{dt^2} + 2n \cos \alpha \frac{dx}{dt} + n^2 x = a \cos nt$ , such that  $x = 0$  and  $dx/dt = 0$  at  $t = 0.$  [6]

**UNIT-V**

Q.5 (a) Solve:

$(1+x)^2 \frac{d^2y}{dx^2} + (1+x) \frac{dy}{dx} + y = 4 \cos \{\log(1+x)\}.$  [8]

(b) Solve:

$\frac{d^2y}{dx^2} + (3\sin x - \cot x) \frac{dy}{dx} + (2\sin^2 x)y = \sin^2 x e^{-\cos x}$  [8]

**OR**

Q.5 (a) Solve:

$(2x^2 + 3x) \frac{d^2y}{dx^2} + (6x + 3) \frac{dy}{dx} + 2y = (x+1)e^x.$  [8]

(b) Solve by the method of variation of parameters-

$x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} - y = x^2 e^x.$  [8]