

Roll No. \_\_\_\_\_

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2E2002

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B.Tech. I Year II Semester (Main) Examination - 2013

202 Engg. Mathematics - II

Time : 3 Hours

Maximum Marks : 80

Min. Passing Marks : 24

**Instructions to Candidates:**

Attempt any **five** questions, selecting **one** question from each **unit**. All questions carry **equal** marks. (Schematic diagrams must be shown wherever necessary. Any data you feel missing suitably be assumed and stated clearly. Units of quantities used/calculated must be stated clearly.)

**Unit - I**

1. a) A sphere of constant radius  $2k$  passes through the origin and meets the axes in points A, B and C. Show that the locus of the centroid of tetrahedron OABC is the sphere  $x^2 + y^2 + z^2 = k^2$ . (8)
- b) Find the equation of a right circular cone generated by the line drawn from origin to cut the circle through the three points  $(1,2,2)$ ,  $(2,1,-2)$  and  $(2,-2,1)$ . (8)

**OR**

1. a) Find the equation of the sphere which touches the plane  $3x + 2y - z + 2 = 0$  at the point  $(1, -2, 1)$  and cuts the sphere  $x^2 + y^2 + z^2 - 4x + 6y + 4 = 0$  orthogonally. (8)
- b) Find the equation of the right circular cylinder having the line  $\frac{x-2}{2} = \frac{y-1}{1} = \frac{z}{3}$  as axis and passing through the point  $(0,0,3)$ . (8)

**Unit - II**

2. a) Solve the following system of equations:

$$5x + 3y + 7z = 4$$

$$3x + 26y + 2z = 9$$

$$7x + 2y + 10z = 5$$

(8)

b) Verify Cayley-Hamilton theorem for the following matrix:

$$A = \begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix} \quad (8)$$

OR

2. a) Find the eigen values and the corresponding eigen vectors of the following matrix.

$$A = \begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix} \quad (8)$$

b) Find the inverse of the matrix by using elementary transformations

$$A = \begin{bmatrix} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{bmatrix} \quad (8)$$

Unit - III

3. a) A particle moves on the curve  $x = 2t^2, y = t^2 - 4t, z = 3t - 5$ , where  $t$  is the time. Find the components of velocity and acceleration at time  $t=1$  in the direction  $\hat{i} - 3\hat{j} + 2\hat{k}$ . (8)

b) If  $\vec{F} = y\hat{i} - x\hat{j}$ , then evaluate  $\int_C \vec{F} \cdot d\vec{r}$  from  $(0,0)$  to  $(1,1)$  along the paths

(i) Parabola  $y = x^2$

(ii) Line from  $(0,0)$  to  $(1,0)$  and then to  $(1,1)$ . (4+4)

OR

3. a) Find  $\text{div } \vec{F}$  and  $\text{Curl } \vec{F}$  where  $\vec{F} = \text{grad}(x^3 + y^3 + z^3 - 3xyz)$ . (4+4)

b) If  $\vec{r}(t) = 5t^2\hat{i} + t\hat{j} - t^3\hat{k}$  then find  $\int_1^2 \left( \vec{r} \times \frac{d^2\vec{r}}{dt^2} \right) dt$  (8)

## Unit - IV

4. a) Using Green's theorem, evaluate  $\int_c [(y - \sin x) dx + \cos x dy]$  where  $c$  is the triangle enclosed by the lines  $y = 0; x = \frac{\pi}{2}; \pi y = 2x$ . (8)

- b) Find Fourier series for the function  $f(x) = \frac{x(\pi^2 - x^2)}{12}$  in  $(-\pi, \pi)$ . (8)

OR

4. a) Use Gauss's divergence theorem to show that  $\iiint_s (x dy dz + y dz dx + z dx dy) = 4\pi a^3$ , where the surface  $S$  is the sphere  $x^2 + y^2 + z^2 = a^2$ . (8)
- b) Find Fourier sine series for the function  $f(x) = e^{ax}$  for  $0 < x < \pi$ . (8)

## Unit - V

5. a) Solve in series.

$$(1 - x^2) \frac{d^2 y}{dx^2} + 2x \frac{dy}{dx} + y = 0 \quad (8)$$

- b) Solve  $2xz + qp = px^2 + 2qxy$ . (8)

OR

5. a) Solve in series  $x \frac{d^2 y}{dx^2} + \frac{dy}{dx} + y = 0$ . (8)

- b) Solve  $x(y^2 + z)p - y(x^2 + z)q = (x^2 - y^2)z$ . (8)

$\downarrow$   
 $\pi$   
 $0$